

5062 - Forces & Energy

Forces - Different types

Constant Forces

F_{app} - Applied force

F_{fr} - Friction force

F_n - Normal force

F_{spring} - Spring force

Forces At A Distance

F_g - Force of Gravity

Other Forces

- Magnetic force
- Electrical forces
- Buoyant forces
- Electromagnetic forces
- Nuclear forces
- Centripetal forces

Jedi forces

Newton's Laws of Motion

- 1.) Inertia - An object rest remains at rest unless acted on by an external unbalanced force.
- 2.) Acceleration - Acceleration is directly proportional to the force applied by an object and indirectly proportional to its mass.

$$a \propto \frac{F}{M}$$

$$F = M \cdot a$$

Units: $(\text{kg} \cdot \text{m} / \text{s}^2)$
Newton (N)

- 3.) Action/Reaction - For every action there is an equal & opposite reaction.

Universal Gravitation

$$F \propto \frac{M_1 M_2}{d^2}$$

$$F = \frac{G M_1 M_2}{d^2}$$

Universal Gravitational Constant
 $G = 6.67 \times 10^{-11} \frac{N \cdot m^2}{kg^2}$

Ex. Calculate the force of attraction between a 2000kg rhino and a 5000kg elephant if they are 3m apart.

$m_1 = 2000 \text{ kg}$
 $m_2 = 5000 \text{ kg}$
 $d = 3 \text{ m}$

$$F = \frac{G M_1 M_2}{d^2}$$

$$F = \frac{(6.67 \times 10^{-11})(2000)(5000)}{3^2}$$

$$F = 7.41 \times 10^5 \text{ N}$$

Ex. Mass of Earth: $5.972 \times 10^{24} \text{ kg}$
 Mass of Sun: $1.989 \times 10^{30} \text{ kg}$
 Distance Earth to Sun: 149,597,870 km
 What is force of attraction?

$$F = \frac{G M_1 M_2}{d^2} = \frac{(6.67 \times 10^{-11})(5.972 \times 10^{24})(1.989 \times 10^{30})}{(149,597,870,000 \text{ m})^2}$$

$$F = 3.54 \times 10^{22} \text{ N}$$

Ex. What is the force of attraction between Marc & the earth

Marc's Mass: 79.18 kg
 Mass of Earth: $5.98 \times 10^{24} \text{ kg}$
 Distance to centre of Earth: $6.37 \times 10^6 \text{ m}$

$$F = \frac{G M_1 M_2}{d^2} = \frac{(6.67 \times 10^{-11})(5.98 \times 10^{24})(79.18)}{(6.37 \times 10^6 \text{ m})^2}$$

← Mass of Marc

$$F = 778 \text{ N}$$

↑ Weight of Marc

↓ 9.8 m/s^2

Note: On Earth: mass = 79kg Weight = 778N
 On Moon: mass = 79kg Weight < 778N
 In space: mass = 79kg Weight = 0N

Free Body Diagrams

- Way to visualize all forces acting on an object.

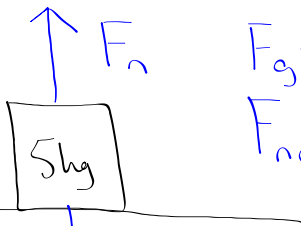
If an object is not moving:

Note:

$$F_g = m \cdot a$$

On earth:

$$F_g = m \cdot g$$



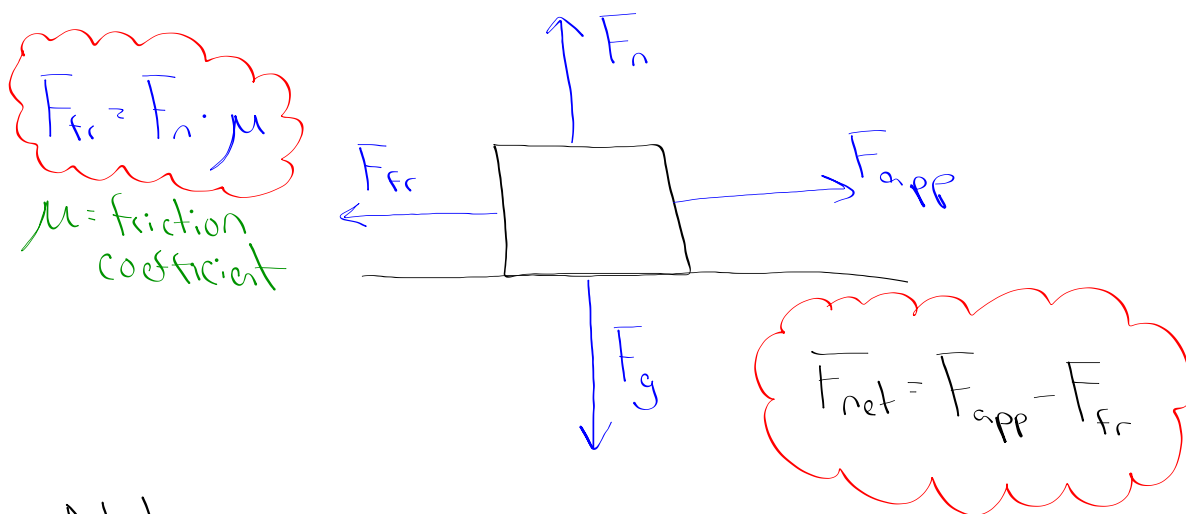
$$F_g = F_n$$

$$F_{net} = 0\text{ N}$$

$$F_g = m \cdot g$$

$$= (5\text{ kg})(9.8\text{ m/s}^2)$$

$$F_g = 49\text{ N}$$



Note:

If an object is at constant speed

$$a = 0 \text{ m/s}^2$$

$$\therefore F_{net} = 0 \text{ N}$$

Once we have F_{net} , we can also find acceleration because $F_{net} = m \cdot a$

Ex. A 10kg container is moving to the right at a constant velocity of 4m/s. It encounters a frictional force of 20N. Analyze all the forces on the object. (Draw a free body diagram)

$$F_{fr} = F_n \cdot \mu$$

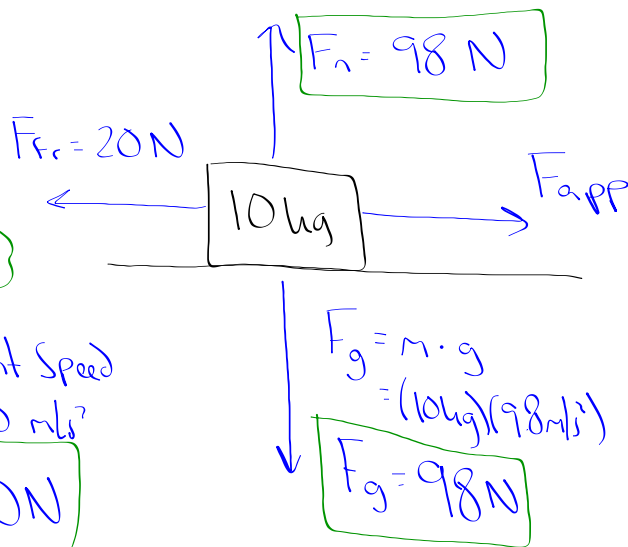
$$\mu = \frac{F_{fr}}{F_n}$$

$$\mu = \frac{20\text{N}}{98\text{N}}$$

$$\mu = 0.204$$

Constant Speed
 $a = 0 \text{ m/s}^2$

$$F_{net} = 0\text{N}$$



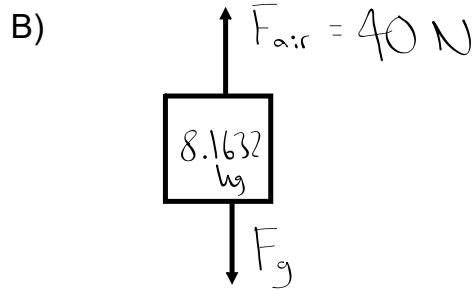
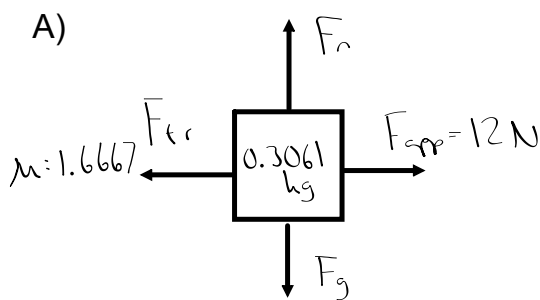
$$F_{net} = F_{app} - F_{fr}$$

$$0 + F_{fr} = F_{app}$$

$$F_{app} = 20\text{N}$$

Ex. A 15kg object is accelerating to the left at 4 m/s^2 . There is a friction coefficient of 0.15. Analyze all the forces on the object.

Ex. 1) For each of the situations determine the net force.



2) A rightward force is applied to a 6kg object to move it across a surface at constant velocity. The object encounters 15N of friction. Analyze all properties on the object.